

## SOLVING QUADRATIC EQUATIONS

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### Lesson Description

In this lesson we:

- Complete the square.
- Solve quadratic equations using factorisation and the quadratic formula



### Summary

#### Quadratic Equations

1. In solving quadratic equations (where the polynomial can be factorised), we will make use of the following property:  
If  $A \cdot B = 0$ , then  $A = 0$  or  $B = 0$ .
2. Quadratic Equations where the polynomial does not factorise;  
Use the quadratic formula if  $ax^2 - bx - c = 0$ :

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

#### Tips for Solving Equations

1. When an equation is NOT linear (that means the highest exponent is not 1), then rewrite the equation in the form of  $ax^2 - bx - c = 0$
2. EQUATE TO ZERO, before solving the equation.



### Test Yourself

#### Question 1

Choose the correct answer

What is the value of  $p$  which makes  $x^2 - x + p$  a perfect square?

- A.  $-\frac{1}{2}$
- B.  $\frac{1}{2}$
- C.  $\frac{1}{4}$
- D.  $-\frac{1}{4}$

**Question 2**

Choose the correct answer

If  $3(x - 3) = 12$ , then  $x = \dots$

- A. 1
- B. 3
- C. 5
- D. 7

**Question 3**

Choose the correct answer

The difference between the roots of  $x^2 + x - 6 = 0$  is

- A. -2
- B. -3
- C. 3
- D.  $\pm 5$

**Question 4**

Choose the correct answer

If  $(y - 3)(x - 2) = 0$  and  $y = 5$  then

- A.  $x = -2$
- B.  $x = 2$
- C.  $x = \frac{5}{2}$
- D.  $x = 0$

**Question 5**

Choose the correct answer

If  $kx^2 - 5x + k = 0$  has 2 as one of its roots, calculate the value of  $k$  and its other root.

- A.  $k = 2$  and  $x = \frac{1}{2}$
- B.  $k = \frac{1}{2}$  and  $x = 2$
- C.  $k = -\frac{1}{2}$  and  $x = -2$
- D.  $k = \frac{1}{2}$  and  $x = -2$

**Question 6**

Choose the correct answer

If  $(x - 3)(2x + 1) = 0$  then  $2x + 1$  has possible values of

- A. 0 only
- B. 0 and 3
- C. 0 and 7
- D.  $-\frac{1}{2}$  and 3

**Question 7**

Choose the correct answer

Solve for  $a$ :  $(3^a - 1)(2^a + 4) = 0$

- A.  $a = 1$  or  $a = -2$
- B.  $a = 0$
- C.  $a = 0$  or  $a = -2$
- D. No solution

**Question 8**

Choose the correct answer

Solve for  $x$ :  $2x - 5x^{\frac{1}{2}} - 3 = 0$

- A.  $x = 9$
- B.  $x = 3$
- C.  $x = \frac{1}{2}$
- D.  $x = \frac{1}{9}$

**Question 9**

Choose the correct answer

If  $p$  is the larger of the roots of  $2x^2 - 3x - 7 = 0$  then  $1 + 3p - 2p^2$  is equal to...

- A.  $3\frac{1}{2}$
- B.  $-6$
- C.  $\sqrt{65}$
- D.  $-\sqrt{47}$

**Question 10**

Choose the correct answer

Solve for  $x$ :

$$(3x + 2)(x - 2) = 2x^2 - 3x + 2$$

- A.  $x = -3$  or  $x = 2$
- B.  $x = -2$  or  $x = 3$
- C.  $x = 2$  or  $x = -\frac{2}{3}$
- D.  $x = 2$  or  $x = -\frac{1}{2}$

**Improve your Skills****Question 1**

Solve for  $x$ , by completing the square and leaving your answer in simplified surd form:

$$-2x^2 + 12x - 8 = 0$$

**Question 2**

Solve for  $x$ :  $2x^3 - 5x^2 - 11x = 0$

**Question 3**

Solve for  $x$ .

Leave your answers in simplified surd form where necessary:

$$(x - 4)^2 = k, \text{ where}$$

- 3.1  $k = 0$
- 3.2  $k = -9$
- 3.3  $k = 5$